The Rofft School

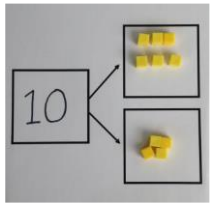
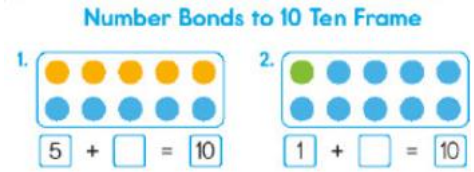
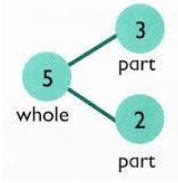
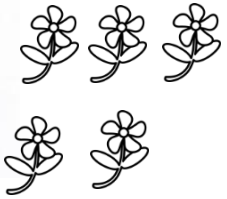
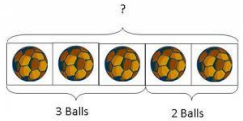
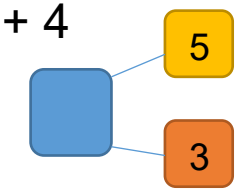
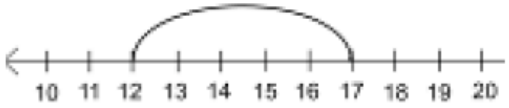
Calculations Policy

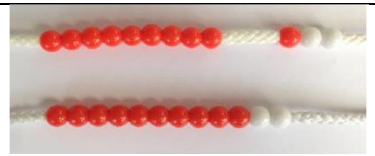
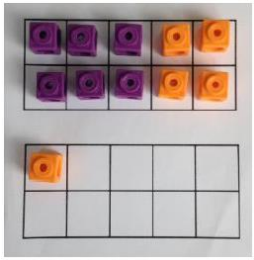
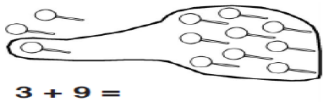
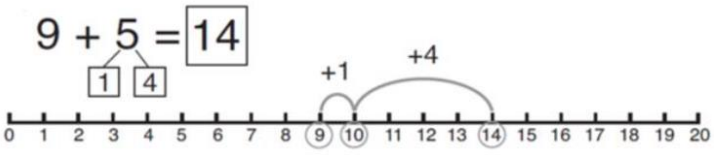
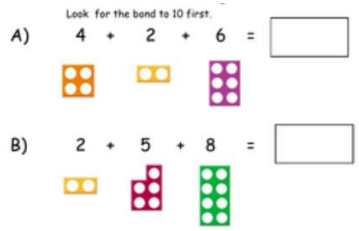
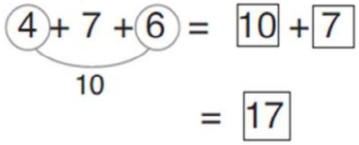
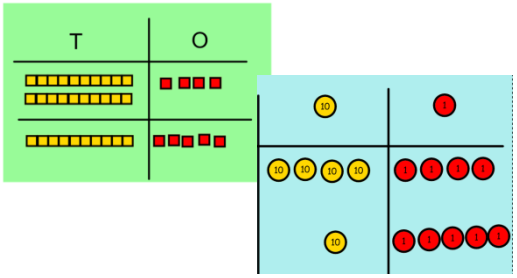
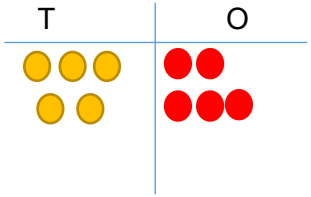
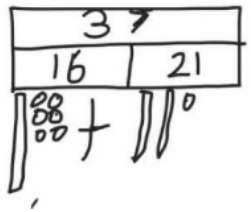
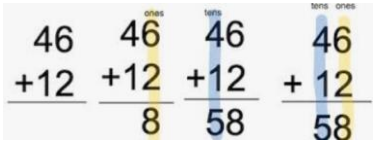
Progression Step Two and Three

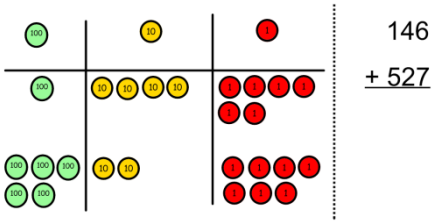
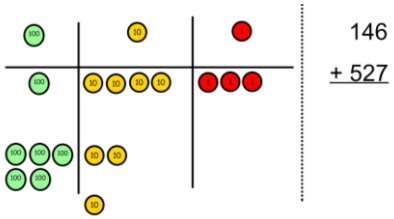
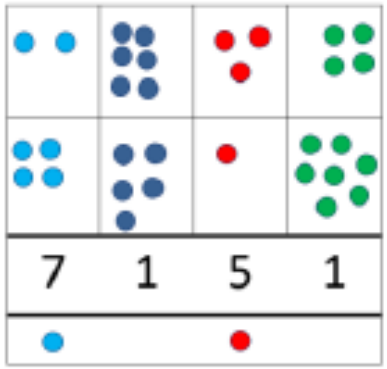
To be used in conjunction with The Rofft's M&N Progression Maps and Abacus Maths

Progression in Calculations

Addition

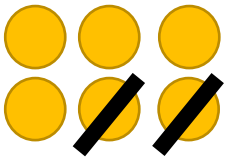
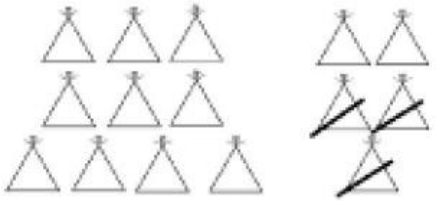
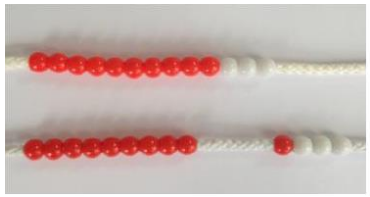
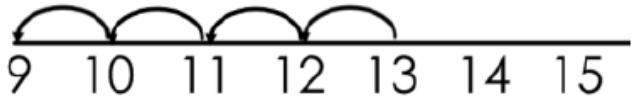
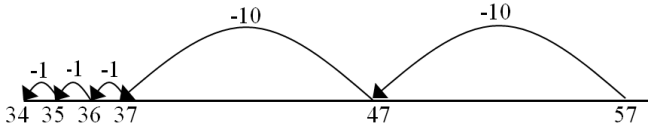
Skill	Concrete	Pictorial	Abstract
Combining two parts to make a whole: part-whole model	 Use cubes, bead strings, ten frames etc to add two numbers together as a group or in a bar. 	   Use pictures to add two numbers together as a group or in a bar.	4 + 3 = 7 10= 6 + 4  Use the part-part whole diagram as shown above to move into the abstract.
Starting at the bigger number and counting on	Start with the larger number on the bead string and then count on the smaller number, 1 by 1, to find the answer. This could also be done using multi-link, counters and ten frames etc.	12 + 5 = 17  Start at the larger number on the number line and count on the smaller number -count in ones or in one jump- to find the answer. This can also be done on a 100 square when dealing with larger numbers.	5 + 12 = 17 Place the larger number in your head and count on the smaller number to find your answer. To progress – Use place value knowledge and understanding to develop mental addition skills.

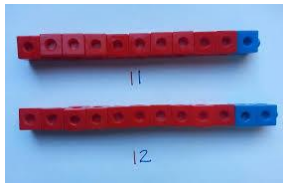
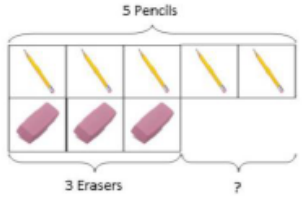
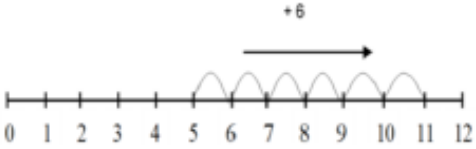
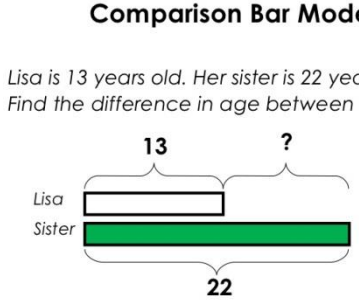
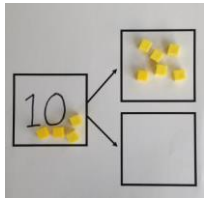
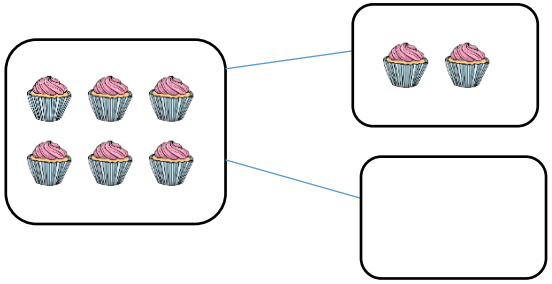
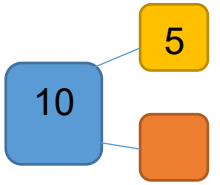
Regrouping to make 10.	 6 + 5 = 11  Start with the bigger number and use the smaller number to make 10.	Use pictures or a number line. Regroup or partition the smaller number to make 10. Focus on bridging ten to improve mental calculations  3 + 9 =  9 + 5 = 14 1 4 +1 +4 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	7 + 4= 11 If I am at seven, how many more do I need to make 10? How many more do I add on next to find the total? Lots of work needed on bridging ten to aid mental calculation skills.
Adding three single digits	4 + 7 + 6= 17 Find the number bond to 10 first e.g. put 4 and 6 together to make 10. Add on 7. Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit. Possible resources: Bead strings, ten frames, multilink and Numicon.	  Look for the bond to 10 first. A) 4 + 2 + 6 = B) 2 + 5 + 8 = Use dice and associated subitising skills to create number bonds and add on the third number. This can also be done using Numicon. E.g. 6 + 4 = 10, 10 + 2 = 12	 4 + 7 + 6 = 10 + 7 10 = 17 Combine the two numbers that make 10 and then add on the remainder.
Column method- no regrouping	24 + 15= Add together the ones first then add the tens. Use the Base 10 blocks first before moving onto place value counters.  	After practically using the base 10 blocks and place value counters, children can draw the counters to help them to solve additions. They can also draw the Dienes pictorially to support their calcultaitons.   	Column addition with no regrouping. Add ones first and then the tens.  46 +12 46 +12 8 46 +12 58 46 + 12 58

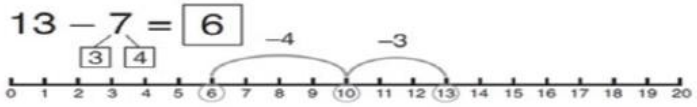
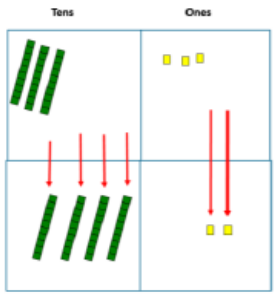
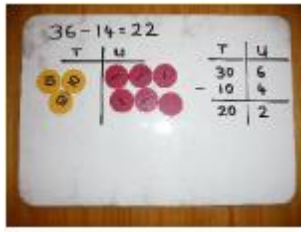
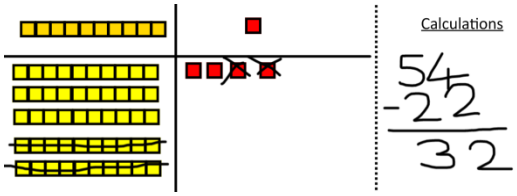
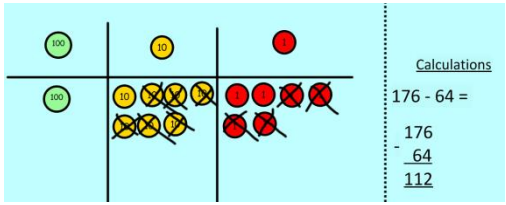
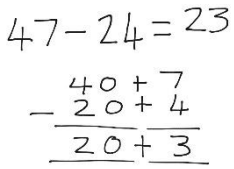
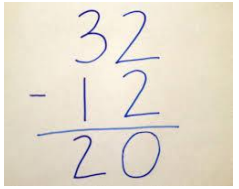
Column method- regrouping	Make both numbers on a place value grid either using place value counters or Dienes.  146 + 527 Add up the units and exchange 10 ones for one 10.  146 + 527 Add up the rest of the columns, exchanging the 10 counters from one column for the next place value column until every column has been added. This can also be done with Base 10 to help children clearly see that 10 ones equal 1 ten and 10 tens equal 100. As children move on to decimals, money and decimal place value counters can be used to support learning.	Children can draw a pictoral representation of the columns and place value counters to further support their learning and understanding. This can also be done using pictorial representations of Dienes resources.  7 1 5 1	Start by partitioning the numbers before moving on to clearly show the exchange below the addition. 20 + 5 40 + 8 60 + 13 = 73 As the children move on, introduce decimals with the same number of decimal places and different. Money can be used here. 72.8 + 54.6 127.4 1 1 £ 2 3 . 5 9 + £ 7 . 5 5 £ 3 1 . 1 4 1 1 1 2 3 . 3 6 1 9 . 0 8 0 5 9 . 7 7 0 + 1 . 3 0 0 9 3 . 5 1 1 2 1 2

536
+ 85
621
1 1

Subtraction

Objective and Strategies	Concrete	Pictorial	Abstract
Taking away ones	Use physical objects, counters, cubes etc to show how objects can be taken away. Use physical resources, fingers etc.  6 – 2 = 4 4 – 2 = 2 	Cross out drawn objects to show what has been taken away.  15 – 3 = 12	18 – 3 = 15 8 – 2 = 6
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 – 4  Use counters and move them away from the group as you take them away counting backwards as you go. 	Count back on a number line or number track  9 10 11 12 13 14 15 Start at the bigger number and count back the smaller number showing the jumps on the number line. E.g. 13 – 4 = 9  -10 -10 -1 -1 -1 34 35 36 37 47 57 This can progress all the way to counting back using two 2-digit numbers. E.g. 57 – 20 – 3 = 34	13 – 4 = 9 Put 13 in your head, count back 4. What number are you at? Use your fingers to help.

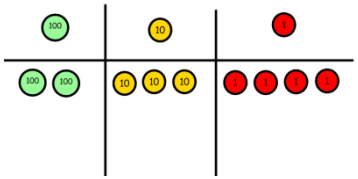
Find the difference	Compare amounts and objects to find the difference.  Use cubes to build towers or make bars to find the difference Use basic bar models/ ten frames with items to find the difference  Numicon can be demonstrated using Numicon. E.g. place the 10 Numicon on the table, sit the 6 Numicon on top, What is left showing if the answer. 10 – 6 = 4 	 Count on to find the difference. Draw bars to find the difference between 2 numbers.  	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches. Children to independently choose the method they want to use and solve mentally and / or using pictures.
Part Whole Model	 Link to addition- use the part whole model to help explain the inverse between addition and subtraction. If 10 is the whole and 6 is one of the parts. What is the other part? 10 - 6 = 4	Use a pictorial representation of objects to show the part whole model. This can also be 	 Move to using numbers within the part whole model.

Make 10	14 – 9 = Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9. This can also be done using the Numicon: 	 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 – 8= How many do we take off to reach the next 10? How many do we have left to take off?
Column method without regrouping	 75 – 42 = 33 Use Base 10 to make the bigger number then take the smaller number away Show how you partition numbers to subtract. Again make the larger number first.  	  Draw the Base 10 or place value counters alongside the written calculation to help to show working.	 This will lead to a clear written column subtraction. 

Column method with regrouping

Use Base 10 (Dienes) to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges.

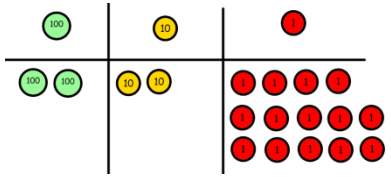
Make the larger number with the place value counters



Calculations

234
- 88

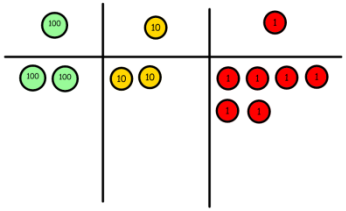
Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.



Calculations

234
- 88

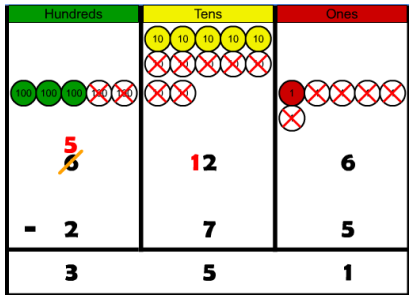
Now I can subtract my ones.



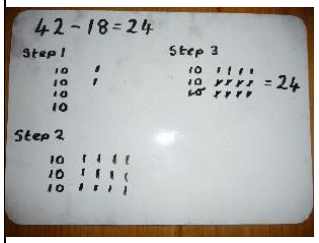
Calculations

234
- 88

Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.

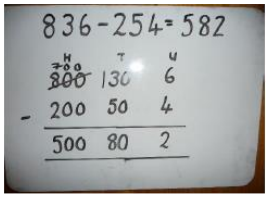


Draw the counters onto a place value grid and show what you have taken away by crossing the counters out as well as clearly showing the exchanges you make.

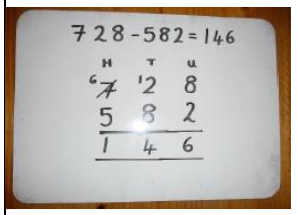


When confident, children can find their own way to record the exchange/regrouping.

Just writing the numbers as shown here shows that the child understands the method and knows when to exchange/regroup.



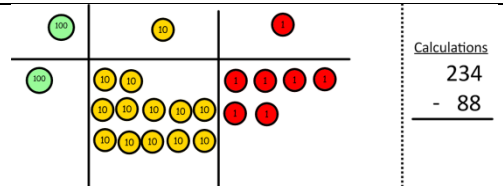
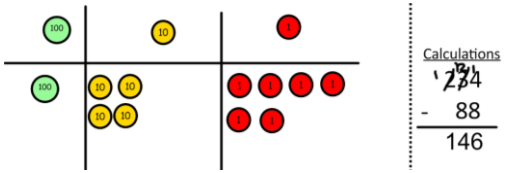
Children can start their formal written method by partitioning the number into clear place value columns.



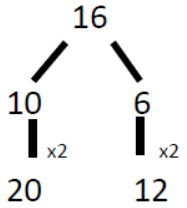
Moving forward the children use a more compact method.

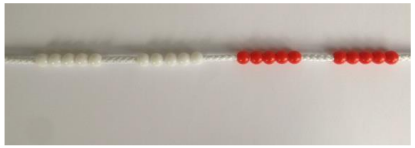
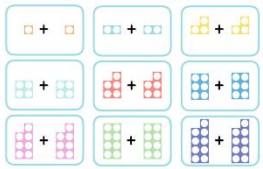
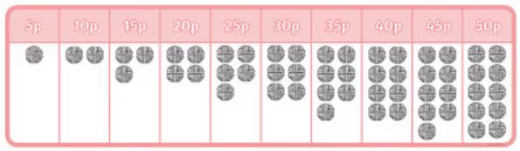
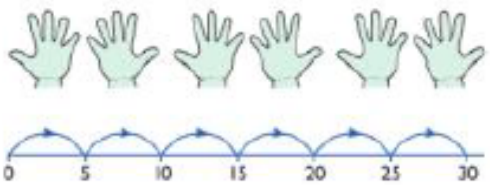
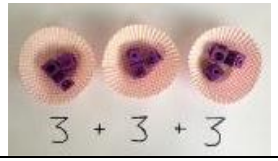
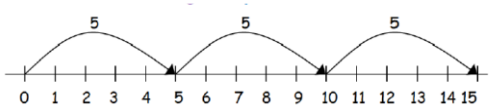
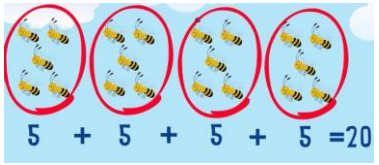
This will lead to an understanding of subtracting any number including decimals.

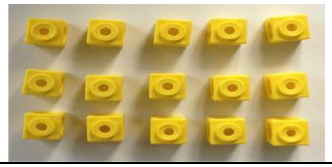
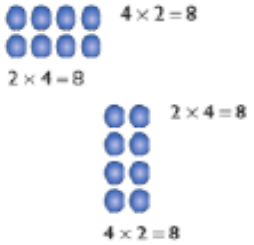
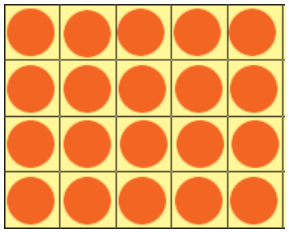
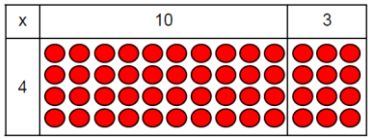
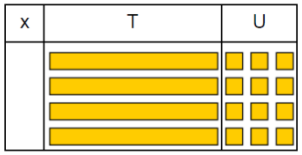
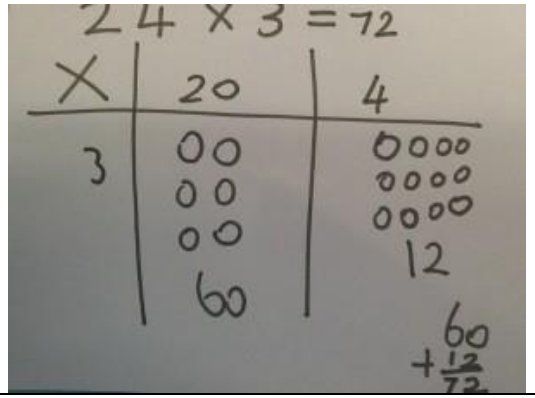
$$\begin{array}{r} {\scriptstyle 5\quad 12\quad\quad 1} \\ 2\ \cancel{6}\ \cancel{3}\ .\ \mathbf{0} \\ -\quad 2\ 6\ .\ 5 \\ \hline 2\ 3\ 6\ .\ 5 \end{array}$$

	 Now I can take away eight tens and complete my subtraction  Show children how the concrete method links to the written method alongside your working. Cross out the numbers when exchanging and show where we write our new amount.		

Multiplication

Objective and Strategies	Concrete	Pictorial	Abstract
Doubling	Use practical activities to show how to double a number. e.g. 5 + 5 = 10 	Draw pictures to show how to double a number. 	 Partition a number and then double each part before recombining it back together. We would also do the same for halving – inverse.

Counting in multiples	   Count in multiples supported by concrete objects in equal groups.	 Use a number line or pictures to continue to support counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25 , 30 4, 8, 12, 16, 20 Use activities such as 'Fizz, Buzz' to embed.
Repeated addition	 Use different objects to add equal groups. 	 5 + 5 + 5 = 15 There are 3 plates. Each plate has 2 star biscuits on. How many biscuits are there? 2 add 2 add 2 equals 6	Write addition sentences to describe objects and picture 2 + 2 + 2 + 2 + 2 = 10  5 + 5 + 5 + 5 =20 s.

Arrays- showing commutative multiplication	Create arrays using counters/ cubes to show multiplication sentences. e.g. 4 x 6 = 24 e.g. 5 x 3 = 15 	Draw arrays in different rotations to find **commutative** multiplication sentences.   Link arrays to area of rectangles. 4cm x 5cm = 20 cm²	Use an array to write multiplication sentences and reinforce repeated addition. 5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15
Grid Method	Show the link with arrays to first introduce the grid method.  4 rows of 10 4 rows of 3 Move on to using Base 10 (Dienes) to move towards a more compact method.  4 rows of 13 Move on to place value counters to show how we are finding groups of a number.We are multiplying by 4 so we need 4 rows.	Children can represent the work they have done with place value counters in a way that they understand. They can draw the counters, using colours to show different amounts or just use circles in the different columns to show their thinking as shown below.  	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. | ×	30	5
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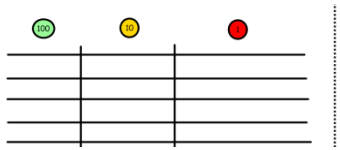
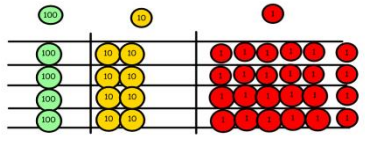
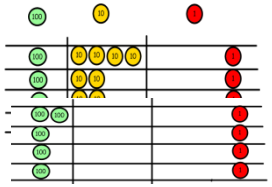
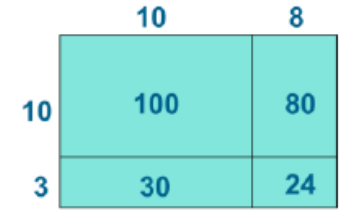
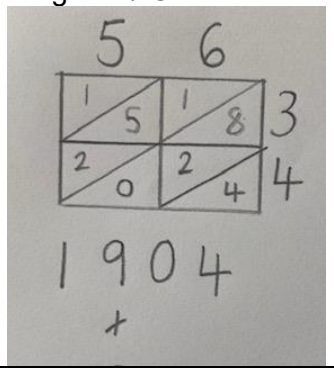
7	210	35	 210 + 35 = 245 Moving forward, multiply by a 2 digit number showing the different rows within the grid method.

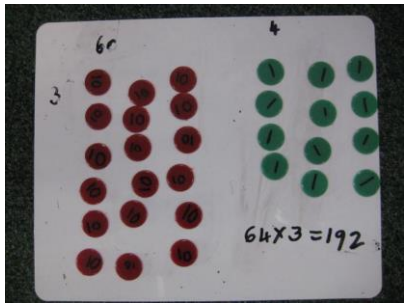
<table>
<tr>
<td></td>
<td>


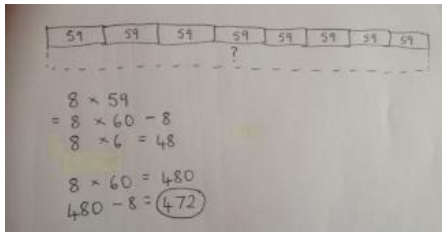
Fill each row with 126.


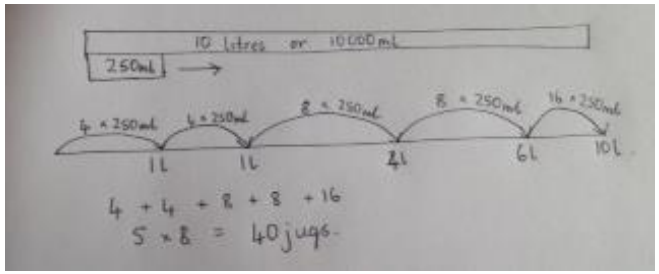
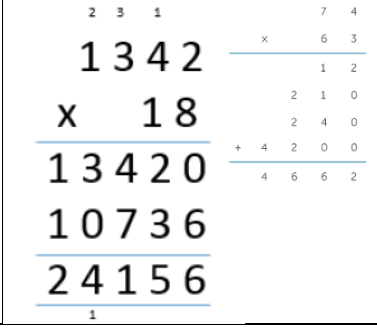
Add up each column, starting with the ones making any exchanges needed.

Then you have your answer.
</td>
<td></td>
<td>


X	1000	300	40	2
10	10000	3000	400	20
8	8000	2400	320	16

Diagonal / Grid Method


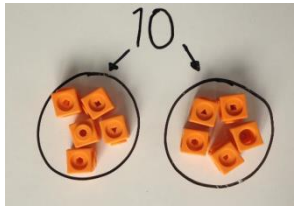
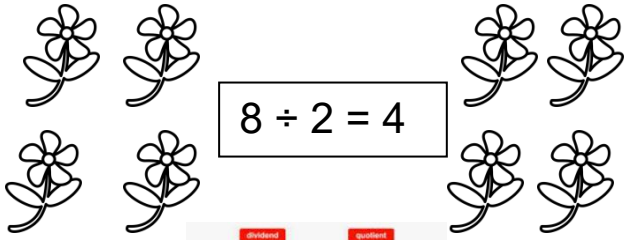
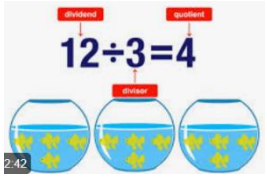
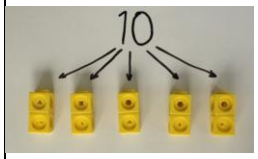
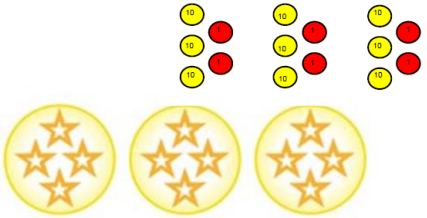
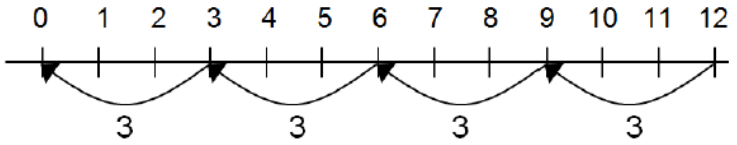
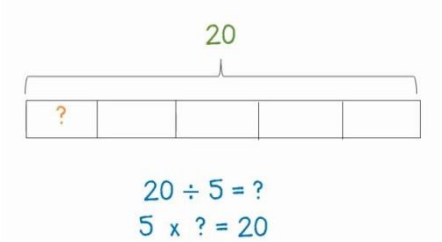
</td>
</tr>
<tr>
<td>Column multiplication</td>
<td>Children can continue to be supported by place value counters at the stage of multiplication.


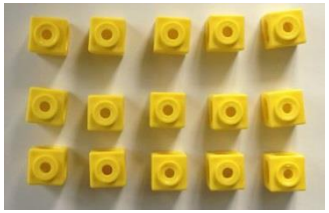
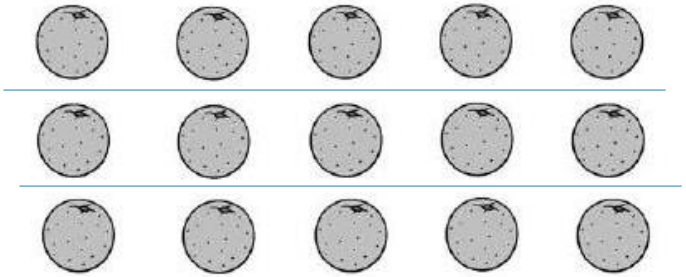
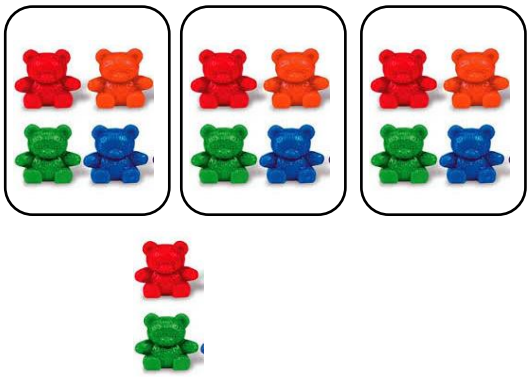
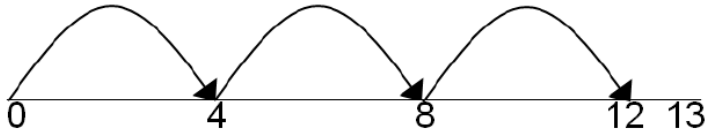
It is important at this stage that they always multiply the ones first and note</td>
<td>Bar modelling and number lines can support learners when solving problems with multiplication alongside the formal written methods.

</td>
<td>Start with long multiplication, reminding the children about lining up their numbers clearly in columns.
If it helps, children can write out what they are solving next to their answer.
324
X 3
12
60
900
972
324
X 3
972</td>
</tr>
</table>

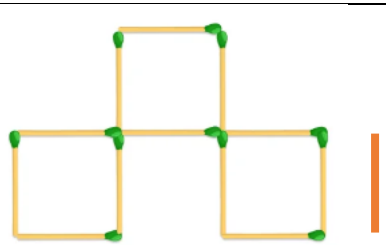
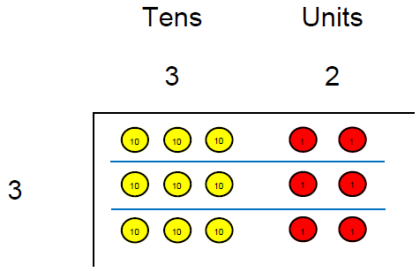
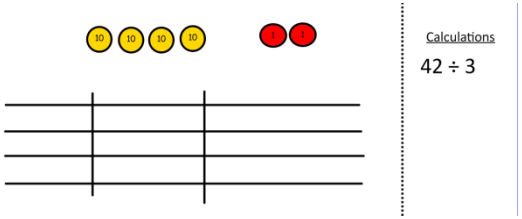
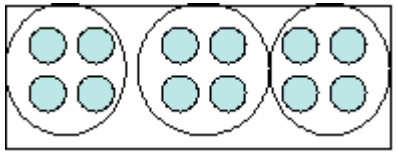
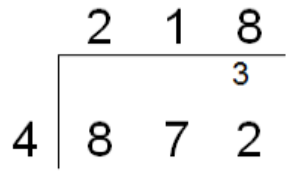
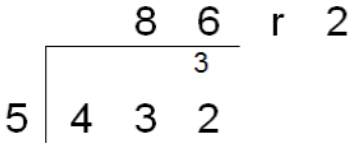
	down their answer followed by the tens which they note below.		32 x 24 8 (4 x 2) 120 (4 x 30) 40 (20 x 2) 600 (20 x 30) 768 This moves to the more compact method. 

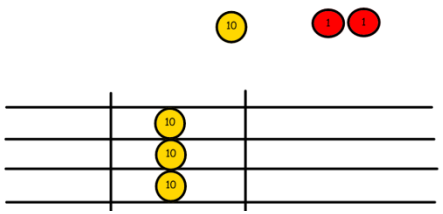
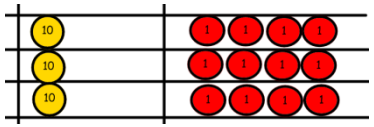
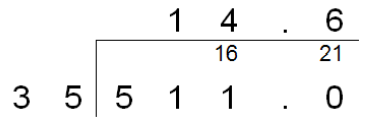
Division

Objective and Strategies	Concrete	Pictorial	Abstract

Sharing objects into groups	 I have 10 cubes, can you share them equally in 2 groups? This can be done using counters, ten frames, Numicon etc. Concentrate on correct sharing e.g. 'one for you, one for you' etc. Physically move the objects. 	Children use pictures or shapes to share quantities.  	Share 9 buns between three people. 9 ÷ 3 = 3 Children to use their knowledge and understanding of multiplication to check their divisions e.g. 9 ÷ 3 = 3 3 x 3 = 9
Division as grouping	Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.  96 ÷ 3 = 32 	Use a number line to show jumps in groups. The number of jumps equals the number of groups.  Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group. Use understanding of multiplication to aid bar modelling work. 	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

Division within arrays	 Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15	 Draw an array and use lines to split the array into groups to make multiplication and division sentences.	Find the inverse of multiplication and division sentences by creating four linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7
Division with a remainder	14 ÷ 3 = Divide objects between groups and see how much is left over 	Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.  Draw dots and group them to divide an amount and clearly show a remainder. Childre to use match sticks to create 2D shapes and use them to work out divisons. Children to also use their understanding of multiplcations to support their learning. 10 ÷ 3 = 3 r1	Complete written divisions and show the remainder using r.

		 13 ÷ 4 = 3r1	
Short division	 Use place value counters to divide using the bus stop method alongside  42 ÷ 3= Start with the biggest place value, we are sharing 40 into three groups. We can put 1 ten in each group and we have 1 ten left over.	Students can continue to use drawn diagrams with dots or circles to help them divide numbers into equal groups.  Encourage them to move towards counting in multiples to divide more efficiently.	Begin with divisions that divide equally with no remainder.  Move onto divisions with a remainder. 

	 We exchange this ten for ten ones and then share the ones equally among the groups.  We look how much in 1 group so the answer is 14.		Finally move into decimal places to divide the total accurately.